

Decomposition Techniques for Social Epidemiology

Advanced Social Epidemiology PhD Course

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Decomposition

1 Life Table Decomposition

2 Concentration Index Decomposition

3 Kitagawa-Blinder-Oaxaca Decomposition

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Overview of Decomposition Techniques

Today:

- Life table decomposition
- Inequality decomposition:
Concentration Index
- Decomposing two-group differences:
Kitagawa-Blinder-Oaxaca

Not covered here:

- Effect decomposition (i.e., mediation)
- Decomposition of population rates
- Inequality decomposition: Indexes for
Nominal social groups

Moving from Description to Explanation

- Ultimately, we want to know why health inequalities are changing over time—what changed?
 - Risk factors?
 - Demographic composition?
 - Social conditions?
- Unpacking the ‘components’ of health inequality is an opportunity to better integrate the monitoring of health inequalities with the etiology of health inequalities.
- These techniques often involve various kinds of ‘counterfactual’ scenarios

3. Decomposition

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Decomposing changes in life expectancy

Uses age- and cause-specific mortality rate differences between two (or more) populations to estimate the contribution of specific age groups and causes of death to changes in life expectancy.

Not causal.

Can provide a means of evaluating 'explanations' for changes in mortality.

Between countries, genders, ethnic groups, social classes, etc.

MEASURING AND EXPLAINING THE CHANGE IN LIFE EXPECTANCIES

Eduardo E. Arriaga

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Abstract—A set of new indices for interpreting change in life expectancies, as well as a technique for explaining change in life expectancies by change in mortality at each age group are presented in the paper. The indices, as well as the new technique for explaining the differences in life expectancies, have been tested and examples using United States life tables are presented. The technique for explaining life expectancy differentials can be used for analyzing change in mortality or mortality differentials by sex, ethnicity, region, or any other subpopulations. The technique can be applied to life expectancies at birth or temporary life expectancies between any desirable ages.

It is well known that an analysis of the general level of mortality of a population based on crude death rates is affected by changes in the population age structure. Consequently, although crude death rates are easy to understand, they are not recommended for determining the pace of mortality change. The problem is partially solved by using standardized crude death rates (standardized by age structure), but the selection of the standard age structure could have some effect on the results. Furthermore, standardized crude death rates would approach a limit (since humans have to die) and therefore problems in interpreting the change would arise.

Life expectancies at birth have frequently been used for analyzing change in mortality. Nevertheless, the measurement and interpretation of life expectancy changes are affected by a problem of relative magnitude. The possible future change of a life expectancy depends on the already achieved level of life expectancies

at birth of about 40 years which did experience increases of over 10 years in life expectancy at birth during a decade. This characteristic of life expectancies (not only at birth but for any age) leads to the problem of how to interpret their change, since it appears easier to achieve a change of 10 years of life expectancies at birth at a level of 40 years of life, than a change of five years at a level of 75 years of life during a similar period of time. Undoubtedly, the possible change in life expectancies is restricted by the limits of the human life span.

In addition to the effect of biological limit on the problem of interpreting a life expectancy change, there is also a technical problem due to unreliable information. Many countries with incomplete death registration systems often report levels of mortality at older ages (usually over 65 years) which are unacceptable or which contain random fluctuations (because of small populations), reflecting

5 Changing Trends in Mortality Decline during the Last Decades

EDUARDO E. ARRIAGA

US Bureau of the Census

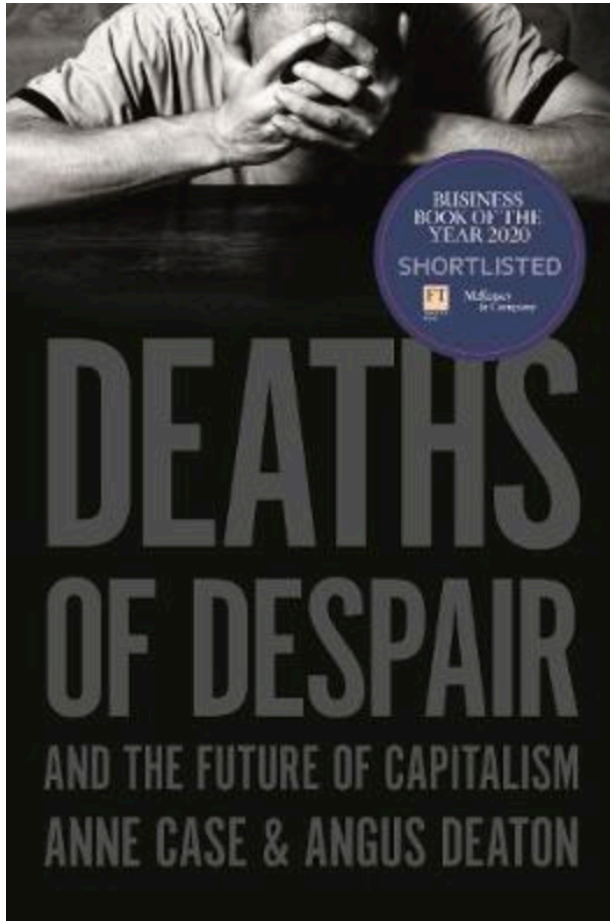
There has been a general concern about recent trends of mortality in developing countries. This concern emerged because in most of the developing countries for which there is information, mortality decline slowed down during the 1960s (as it also did in some developed countries). Data from most of these countries had shown significant gains in life expectation at birth during the 1950s; hence, optimistic predictions of future trends of mortality were made. However, life-tables for some developing countries in the early 1970s showed that the expected fast pace of mortality decline had not continued during the 1960s. Those populations for which information was available had mortality rates during the 1950s which declined rapidly at practically all ages, but during the 1960s most of the gain in life expectation was due to the reduction of infant mortality. At adult ages male mortality rates were only slightly reduced, or, in some countries, even tended to increase (Arriaga, 1981; Sivamurthy, 1981).

As a result of massive programmes for reducing 'excess' mortality during the 1950s, the age pattern of mortality decline in most developing countries was rather similar. Public health programmes were focused on infectious and contagious diseases. Consequently, the number of deaths from those were reduced in most of the countries, and hence the pattern of mortality change by age was also similar. Such similarities in the pattern of mortality decline did not continue during the 1960s. This situation generated several questions. For instance, was the slowing down of mortality decline a real phenomenon, or was it the consequence of the indices used for measuring the change of mortality? Do those developing countries with available information (the only ones than can be analysed) represent the 'developing countries' of the world? If there was indeed a slowing down of mortality decline in developing countries, was this an inevitable mortality trend? Since more information is now available for some countries, this chapter reviews mortality trends in a few developing countries. First, an attempt is made to

The author wishes to thank staff members of the Center for International Research who made valuable comments; Janet Sales, who typed several drafts; and Vivian Cash, who prepared the input data for the computer runs and prepared some of the tables in this chapter.

See Arriaga (1984, 1989) for details.

Example from recent events



Over the last century, Americans' life expectancy at birth has risen from 49 to 77. Yet in recent years, that rise has faltered. Among white people age 45-54 — or a time many view as the prime of life — deaths have risen.

Especially vulnerable are white men without a four-year bachelor's degree. Curiously, midlife deaths have not climbed in other rich countries, nor, for the most part, have they risen for American Hispanics or blacks.

NY Times Book Review, March 17, 2020

Specific causes are a key part of this narrative

Although the surge in deaths in America is what we might see during the ravages of an infectious disease, like the Great Influenza Pandemic of 1918, this is an epidemic that is not carried by a virus or a bacterium, nor is it caused by an external agent, such as poisoning of the air or the fallout from a nuclear accident. Instead, people are doing this to themselves. **They are drinking themselves to death, or poisoning themselves with drugs, or shooting or hanging themselves.**

Case and Deaton (2019, p38)

Example of using life table decomposition



Annual Review of Public Health

Declining Life Expectancy in the United States: Missing the Trees for the Forest

Sam Harper,^{1,2,3} Corinne A. Riddell,⁴ and Nicholas B. King^{1,2,5}

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Decompose the decline in life expectancy in the US between 2014 and 2017

- By age
- By cause of death
- For 8 race-ethnic groups

Annu. Rev. Public Health 2021. 42:381–403

First published as a Review in Advance on December 16, 2020

Keywords

life expectancy, opioids, cardiovascular diseases, suicide, homicide, health inequalities

What are we explaining?

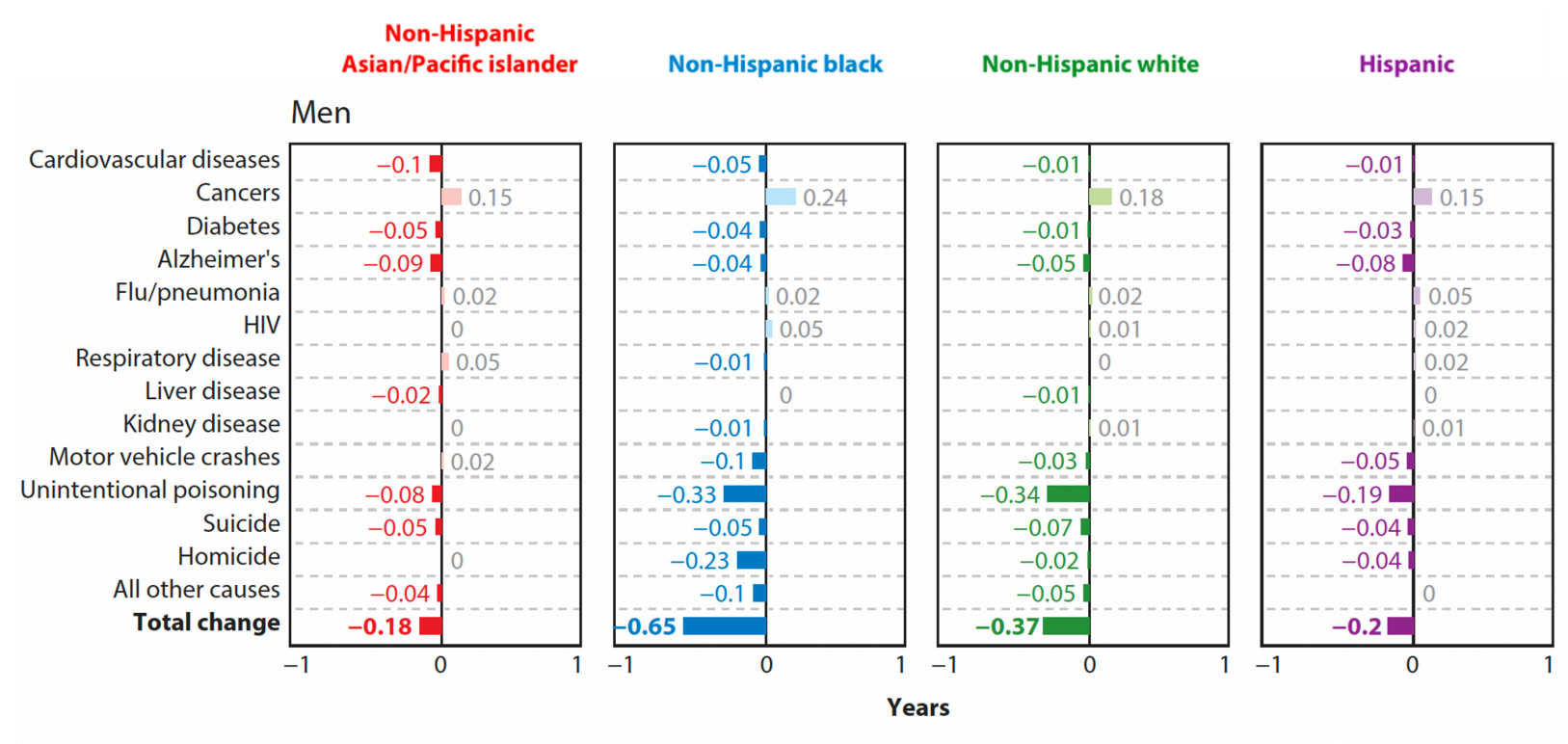
Year	Non-Hispanic API		Non-Hispanic Black		Non-Hispanic White		Hispanic	
	Women	Men	Women	Men	Women	Men	Women	Men
2014	90.0	85.5	78.8	72.7	81.3	76.6	86.3	81.3
2015	89.7	85.4	78.8	72.4	81.1	76.5	86.3	81.2
2016	89.7	85.5	78.6	72.1	81.2	76.3	86.4	81.1
2017	89.7	85.3	78.8	72.0	81.1	76.3	86.4	81.1
2018	90.0	85.5	78.8	72.0	81.3	76.4	86.5	81.0
Changes								
2014-2017	-0.3	-0.2	0.0	-0.7	-0.2	-0.3	0.1	-0.2

Declines evident for all men and for most women

Largest for black men

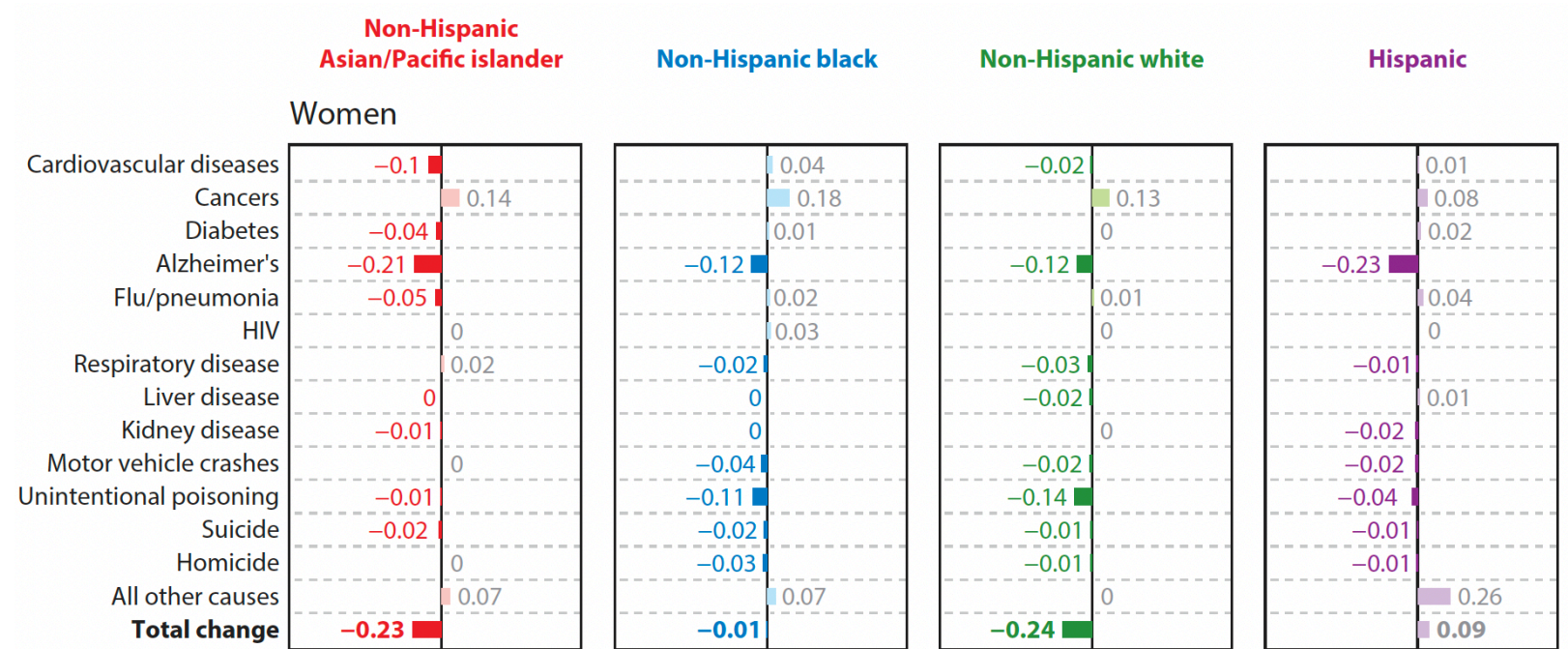
Results by cause: Men

- Opioids (unintentional overdoses) played a large part.
- Homicide for black men
- Little role for suicide or alcohol.



Results by cause: Women

- Opioids, but also Alzheimer's.
- Variations by race-ethnicity
- Cancer mortality improved.



Summary

Life table decomposition useful for understanding links between proximal risks and mortality, and how they may 'explain' changing patterns of life expectancy.

Minimal assumptions, but not causal.

Example showing how the 'Deaths of Despair' narrative is hard to reconcile with diverse mortality patterns:

- Declines have affected all race-ethnic groups.
- Most of the decline due to opioid overdoses, homicide, and Alzheimer's disease.
- Deaths from suicide and alcohol-related causes have risen but explain little of America's stagnating life expectancy trends.

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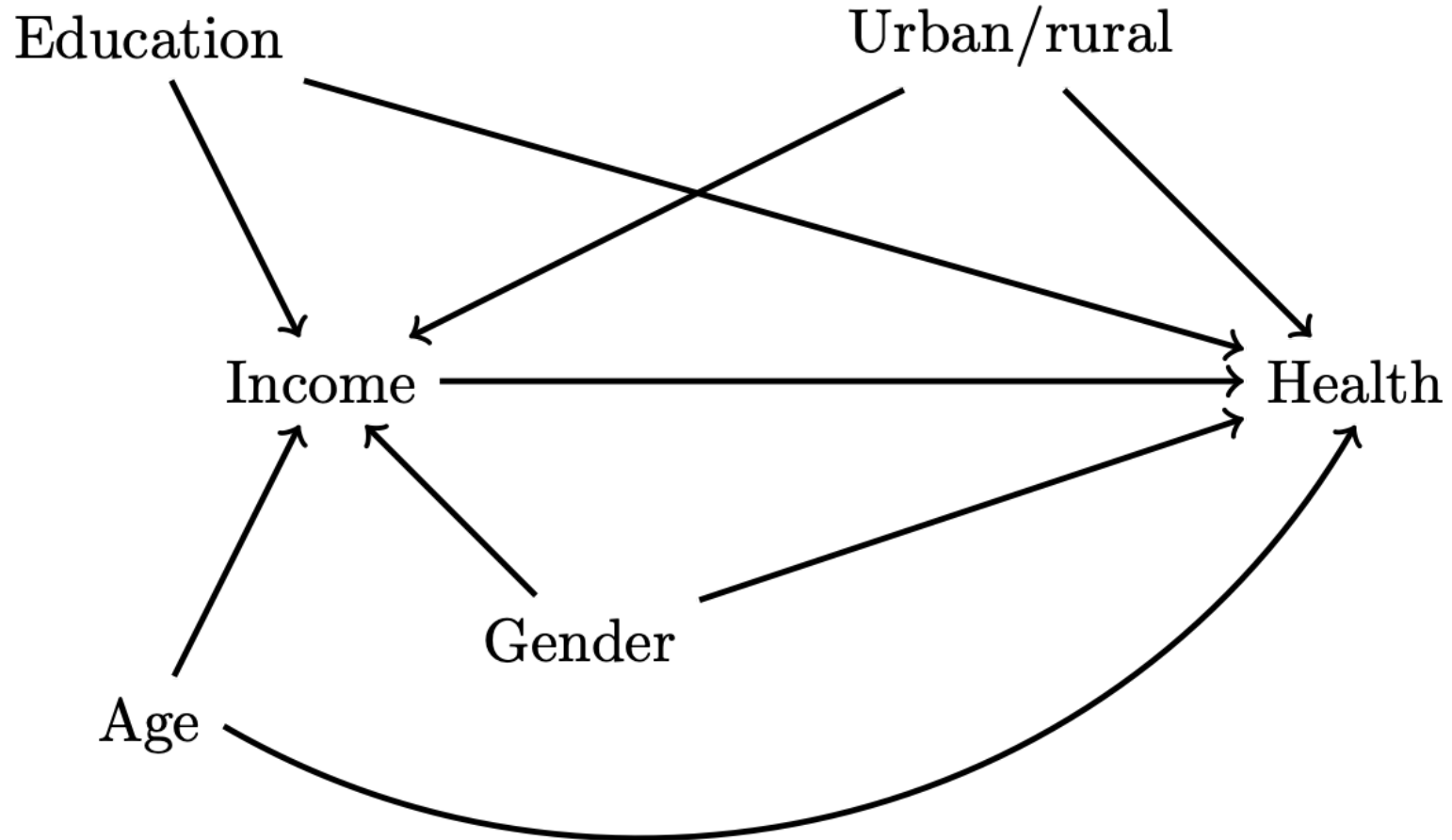
We want to understand this:



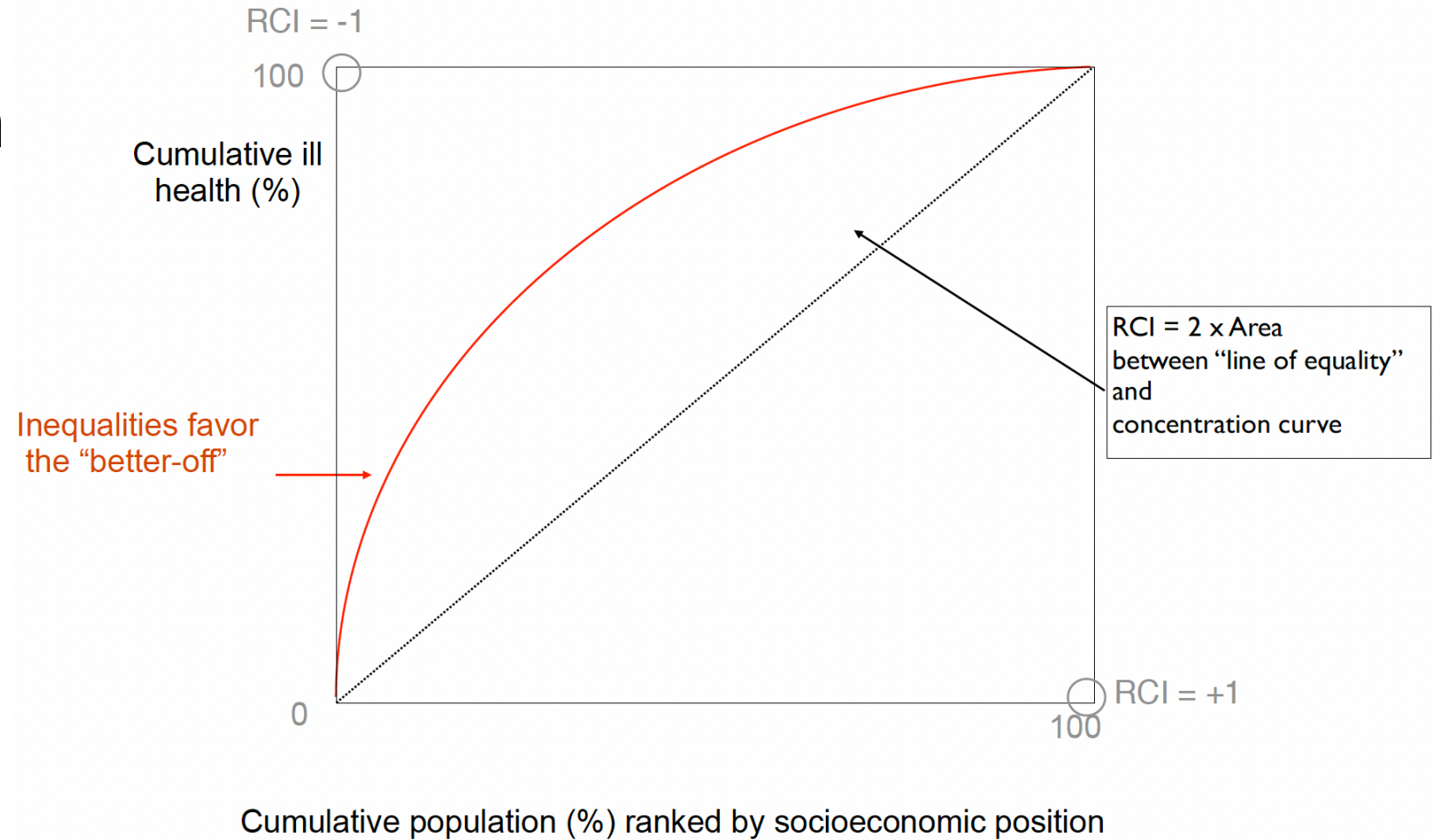
We want to understand this:



By estimating something like this:



Relative Concentration Curve



Formula for writing the Concentration Index

Recall that we can write the CI as:

$$RCI = \frac{2}{n\mu} \sum_{i=1}^n y_i R_i - 1$$

where μ is the mean of y_i (e.g., smoking status), R_i is the fractional rank of the i th person in the socioeconomic (i.e., income) distribution.

The basic idea here is to develop a model for predicting y using several determinants, then plug that model back into the equation for the RCI

Decomposition of the RCI

Since the RCI is a function of health (y_i) and a socioeconomic rank variable (R_i), i.e.

$$RCI = \frac{2}{n\mu} \sum_{i=1}^n y_i R_i - 1$$

Then suppose that one can write a regression equation expressing the health outcome of interest (y_i) as a function of several k_i determinants (e.g., age, gender, urban/rural status):

$$y_i = \alpha + \sum \beta_x x_{k_i} + \epsilon_i$$

Decomposition of the RCI

Since RCI is a function of y_i and socioeconomic rank, one can then re-express the concentration index as:

$$RCI = \sum (\beta_k \bar{x}_k / \mu) RCI_k + gRCI_e / \mu$$

Where

- μ is the mean of y ,
- \bar{x}_k is the mean of x_k ,
- β_k is the regression coefficient for x_k , and
- RCI_k is the concentration index for x_k .

The basic idea: how much of the overall inequality is due to other factors that are both differentially distributed by x (income) and also affect y (e.g., smoking)?

Explained and unexplained components

This equation results in 2 components of socioeconomic inequality:

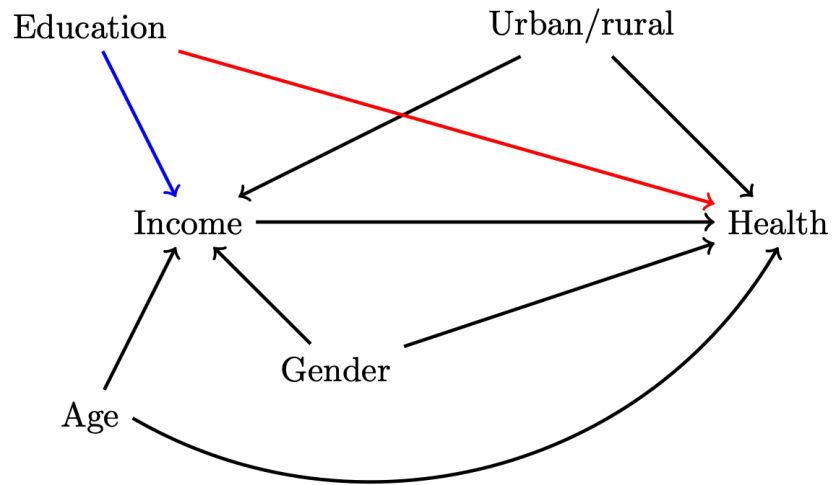
$$RCI = \sum (\beta_k \bar{x}_k / \mu) RCI_k + gRCI_e / \mu$$

One part $(\beta_k \bar{x}_k / \mu) RCI_k$ that is due to the association between income and other factors that predict health

The other part $(gRCI_e / \mu)$ is 'unexplained', i.e., inequality that cannot be explained by systematic variation across income groups in the determinants of health.

Two types of 'explained' components

Income → Health



The influence of determinants depends on two things:

$$RCI_k$$

the strength of the relationship between each factor and income (C_k)

$$\beta_k \bar{x}_k / \mu$$

the strength of the relationship between each factor and health, and its prevalence in the population (elasticity).

Procedure for decomposing the Concentration Index

1 Estimate a regression equation predicting y ('health') from its determinants ($\beta_k x_k$):

$$y_i = \alpha + \sum \beta_x x_{k_i} + \epsilon_i$$

2 Calculate the mean of y (μ) and of each of the determinants (e.g., education, age)

3 Calculate the Concentration Index for the health variable (C) *and* for each determinant in the equation predicting health (C_k).

- That is, use each determinant x_k as the "outcome" and estimate a CI for age, CI for education, etc.

Procedure for decomposing the Concentration Index

4 Calculate the absolute contribution of each determinant by multiplying its 'elasticity' by its concentration index (C_k):

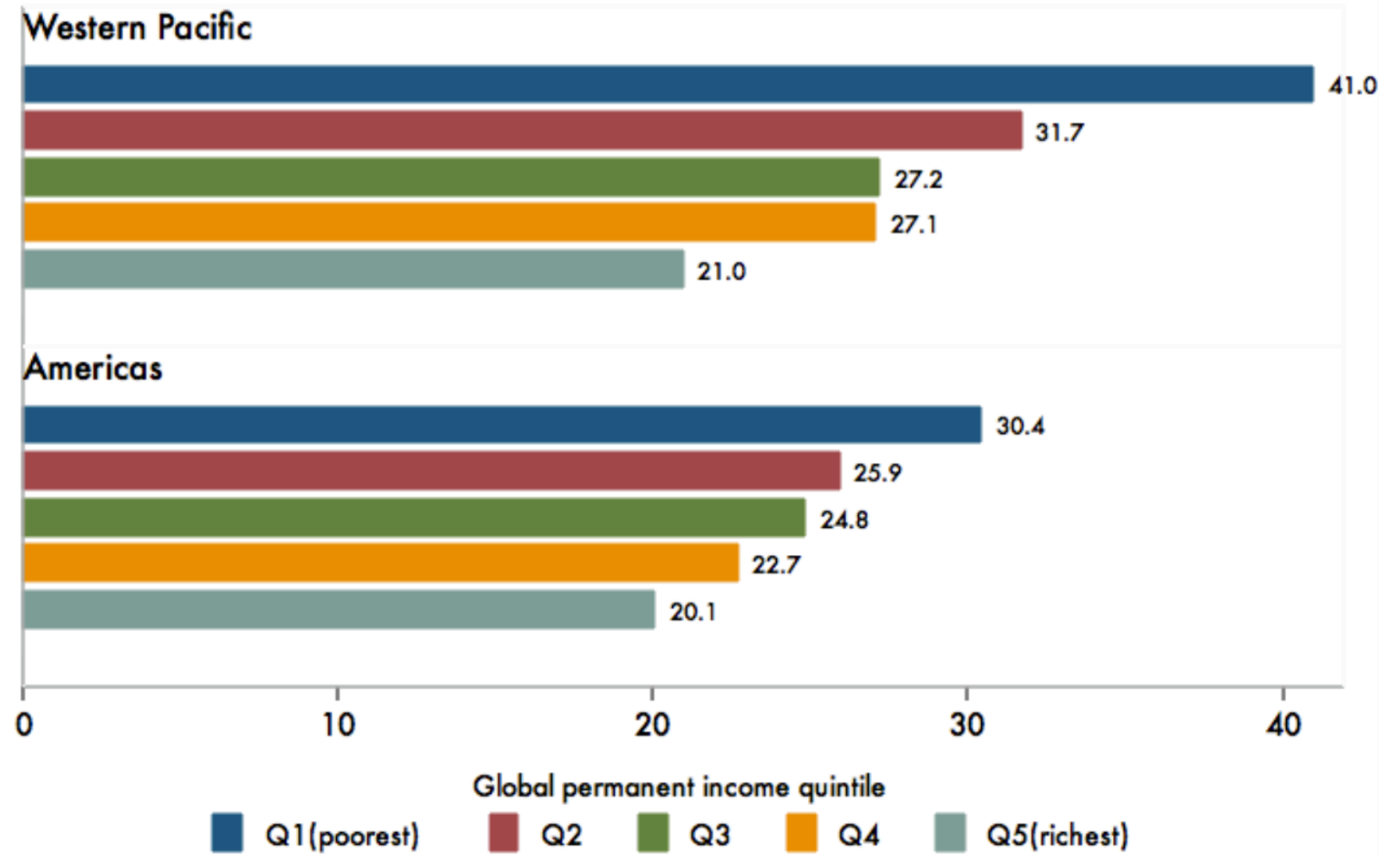
$$(\beta_k \bar{x}_k / \mu) RCI_k$$

5 Calculate the percentage contribution of each determinant:

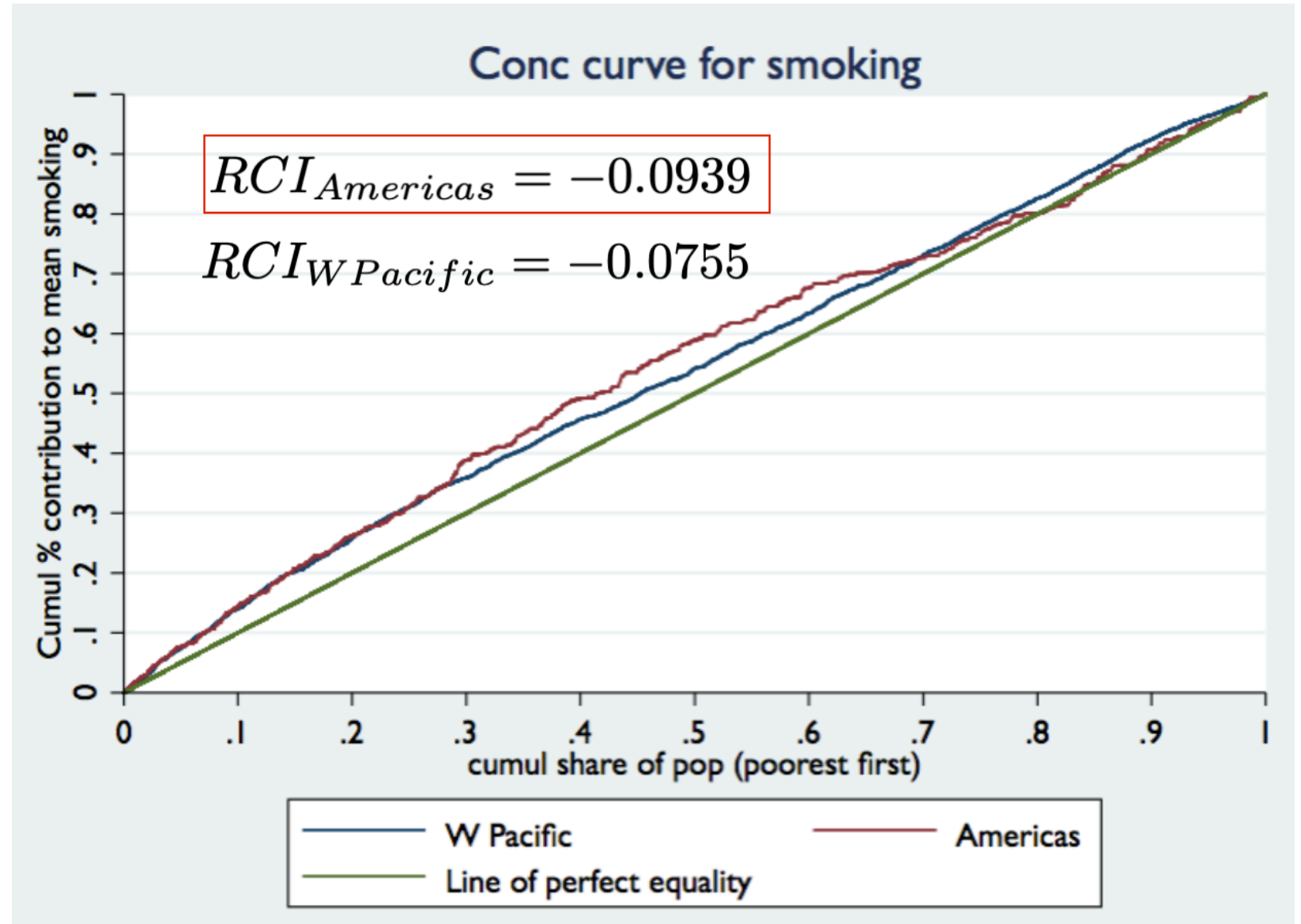
$$[(\beta_k \bar{x}_k / \mu) RCI_k] / RCI$$

Example: Decomposing Socioeconomic Inequality in Current Smoking

Smoking by income quintile



Concentration curve for smoking



Estimation for
a specific
factor:
Education

Recall the decomposition formula:

$$RCI = \sum (\beta_k \bar{x}_k / \mu) RCI_k + g RCI_e / \mu$$

- Estimated β coeff on education (logit scale): -.0389 (OR = 0.96)
- Marginal effect on probability scale: -.0051 (0.5 pct points)
- Mean education: 8.9 yrs
- Mean smoking rate: 17.5%

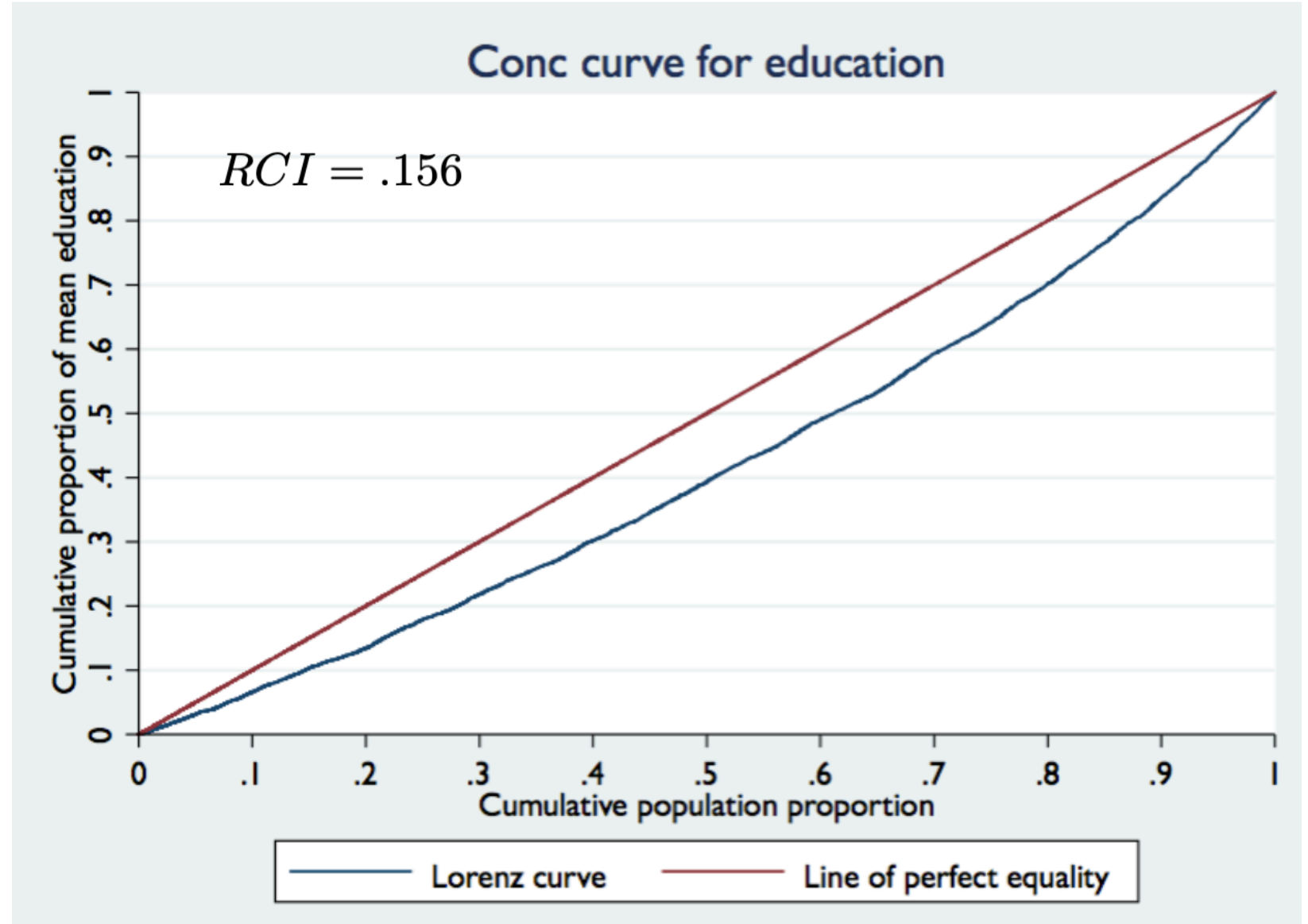
With these parameters, the elasticity of smoking with respect to education is: $(-.0051 * 8.9 / .175) = -.2582$

Interpretation: a 1% increase in education decreases smoking by 26% (not percentage points!).

What about the RCI for education?

Concentration curve for education

Note the y-axis is cumulative share of *education*



Estimation for
a specific
factor:
Education

Recall the decomposition formula:

$$RCI = \sum (\beta_k \bar{x}_k / \mu) RCI_k + gRCI_e / \mu$$

So the **elasticity of smoking** (from the previous slide) with respect to education is $(-.0051 * 8.9 / .175) = -.2582$

Now we have the **RCI for education** = 0.156

So now we can calculate the contribution of education as:

$$\text{Elasticity} \times RCI_{ed} = -.2582 * .156 = -.04$$

Thus education accounts for $-.04 / -.0939 = 41.6\%$ of the overall *RCI*

Decomposition of
Income-Related
Inequality in
Smoking:
Americas region

Overall RCI =
-0.094

	Elasticity	Rel Conc Index	Contribution	% Contrib
Age	3.695	0.023	0.084	-89.9%
Age ²	-1.981	0.032	-0.064	67.9%
Male	0.197	-0.055	-0.011	11.5%
BMI	-0.834	0.011	-0.009	9.6%
Urban	0.020	0.076	0.002	-1.6%
Single	0.078	-0.036	-0.003	3.0%
Divorced/Widowed	0.161	-0.120	-0.019	20.7%
Low Phys Activity	0.057	0.069	0.004	-4.2%
Mod Phys Activity	-0.023	0.025	-0.001	0.6%
Low Alcohol Consumption	0.131	0.123	0.016	-17.1%
Mod/Hi Alcohol Consumption	0.019	0.081	0.002	-1.6%
Low Fruit/Veg Consumption	0.029	-0.066	-0.002	2.0%
Self-Reported Health Good	-0.001	0.040	0.000	0.1%
Self-Reported Health Moderate	-0.043	-0.079	0.003	-3.6%
Self-Reported Health Bad/Very Bad	0.004	-0.208	-0.001	0.9%
Education	-0.250	0.156	-0.039	41.6%
Permanent Income	-0.809	0.054	-0.044	46.4%
Residual			-0.013	

Caveats for decomposing the RCI

Decomposition results will be sensitive to the choice of determinants included (i.e., how well-specified the model is for predicting y).

The regression equations are predictive and not causal models.

Main utility is not in estimating the potential impact on y of changing the distribution of socioeconomic position, but in indicating the potential role that other factors may play in generating socioeconomic inequalities in health.

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Idea for Decomposition of Means

The core idea is to explain the distribution of the outcome variable in question by a set of factors that vary systematically with exposure status.

Thus, we want to know, on average, **why the mean level of health or disease differs between exposed and unexposed groups.**

Since, for most health outcomes there are multiple determinants, we may want to know which of these determinants plays more or less important roles in explaining the difference in average outcomes.

“Unpacking” or “decomposing” difference.

Origins

COMPONENTS OF A DIFFERENCE BETWEEN TWO RATES*

EVELYN M. KITAGAWA

University of Chicago and Scripps Foundation

WHEN comparing the incidence of some phenomenon in two or more groups, social researchers place much emphasis on the need for holding constant those related factors that would tend to distort the comparison. For example, before comparing the death rates for the residents of two areas, demographers frequently control the factors of differences between the areas in age, sex and race composition. A technique commonly used to accomplish this is "standardization" of the rates for the two areas by relating them both to a standard population with specified age-sex-race composition. By applying the schedule of age-sex-race specific death rates for each of the groups to the age-sex-race composition of the standard population, then noting the total death rate that results, it is possible to compare the death rates for the areas with reasonable confidence that differences in age, sex and race composition do not explain the differences between the rates for the areas that still remain after they have been standardized. Controlling the effect of related factors by this method is termed direct standardization.¹

Evelyn Kitagawa was sociologist and demographer who devised a non-parametric method (1955) for decomposing differences between rates, refined by Prithwis das Gupta in 1978.

- Focused on understanding group contributions to rate differences.

Studies by Oaxaca (1973) and Blinder (1973) applied regression-based decomposition methods to analyze the wage gap between men and women and between whites and blacks in the USA.

- Focused on how much of wage gap was 'explained' by differences in observable characteristics

Brief note on interpretation

Decomposition methods are based on regression analyses, and thus all of the usual caveats about good specification apply

If regressions are purely descriptive, they reveal the associations that characterize the health inequality. Then inequality is explained in a statistical sense but implications for policies to reduce inequality are limited.

If data allow identification of causal effects, then the factors that generate the inequality are identified.

Then one can (potentially) draw conclusions about how policies would impact on inequality.

Inequalities in the use of health services between immigrants and the native population in Spain: what is driving the differences?

Dolores Jiménez-Rubio · Cristina Hernández-Quevedo

Abstract In Spain, a growing body of literature has drawn attention to analysing the differences in health and health resource utilisation of immigrants relative to the autochthonous population. The results of these studies generally find substantial variations in health-related patterns between both population groups. In this study, we use the Oaxaca-Blinder decomposition technique to explore to what extent disparities in the probability of using medical care use can be attributed to differences in the determinants of use due to, e.g. a different demographic structure of the immigrant collective, rather than to a different effect of health care use determinants by nationality, holding all other factors equal. **Our findings show that unexplained factors associated to immigrant status determine to a great extent disparities in the probability of using hospital, specialist and emergency services of immigrants relative to Spaniards, while individual characteristics, in particular self-reported health and chronic conditions, are much more important in explaining the differences in the probability of using general practitioner services between immigrants and Spaniards.**

Kitagawa-Blinder-Oaxaca: Basic Idea

Two potential sources of mean differences in outcomes

1. Means

Differences in the prevalence of determinants of outcome

2. Coefficients

Differences in the coefficient of a given determinant on the outcome (i.e., effect measure modification)

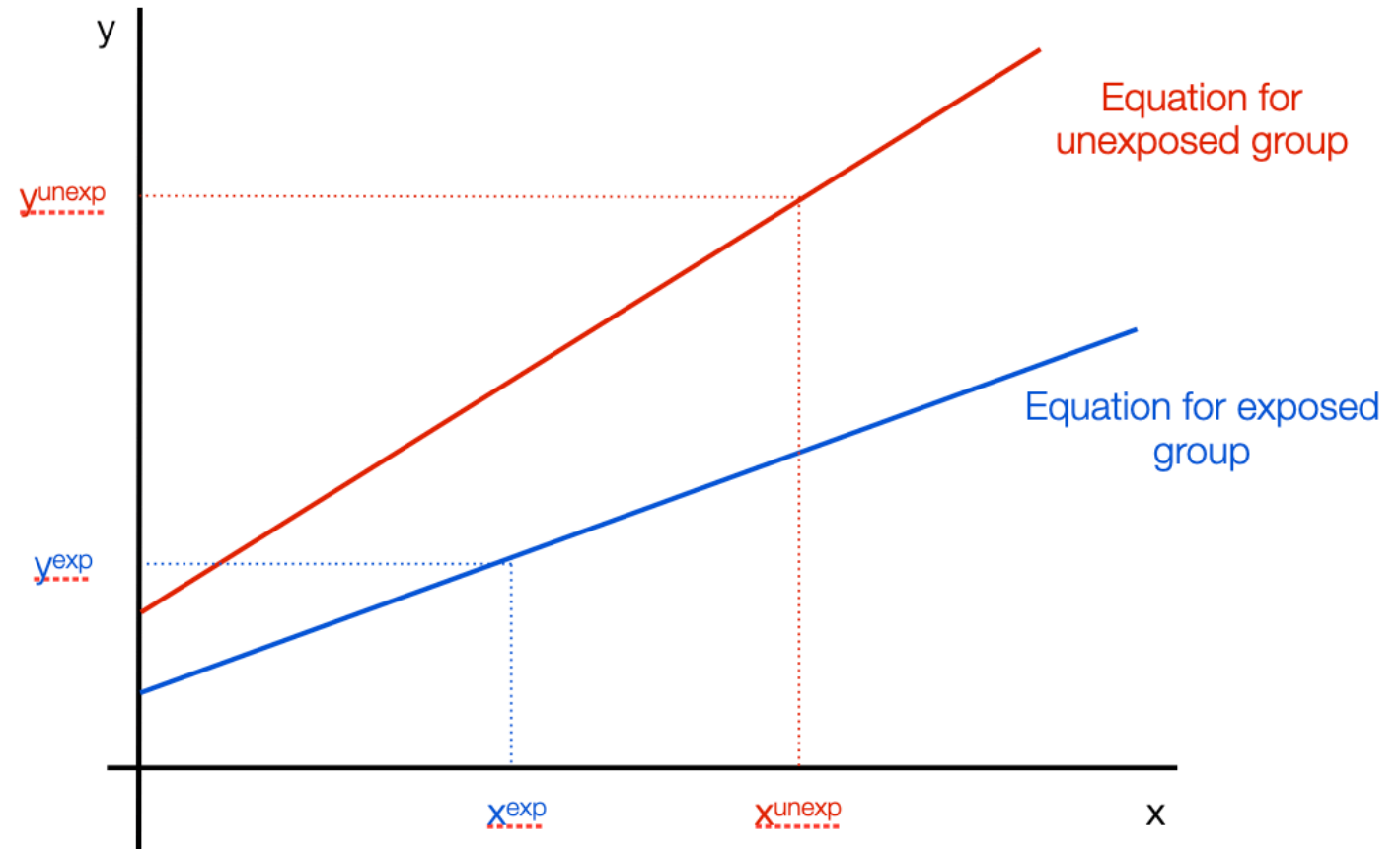
Think of 2 regressions for a given determinant X :

1. Exposed
2. Unexposed

Each generates its own coefficient and uses its own mean.

Use these to generate counterfactuals.

$$y_i = \left\{ \begin{array}{l} \beta^{\text{exp}} x_i + \varepsilon_i^{\text{exp}} \text{ if exposed} \\ \beta^{\text{unexp}} x_i + \varepsilon_i^{\text{unexp}} \text{ if unexposed} \end{array} \right\}$$



Two ways of expressing the mean difference in y

The overall gap between exposed and unexposed can be written as a function of differences the respective beta coefficients, evaluated at the mean for each group:

$$y^{exp} - y^{unexp} = \beta^{exp} \bar{x}^{exp} - \beta^{unexp} \bar{x}^{unexp}$$

This way:

$$y^{exp} - y^{unexp} = \Delta \bar{x} \beta^{unexp} + \Delta \beta x^{exp}$$

where $\Delta \bar{x} = \bar{x}^{exp} - \bar{x}^{unexp}$ and $\Delta \beta = \beta^{exp} - \beta^{unexp}$

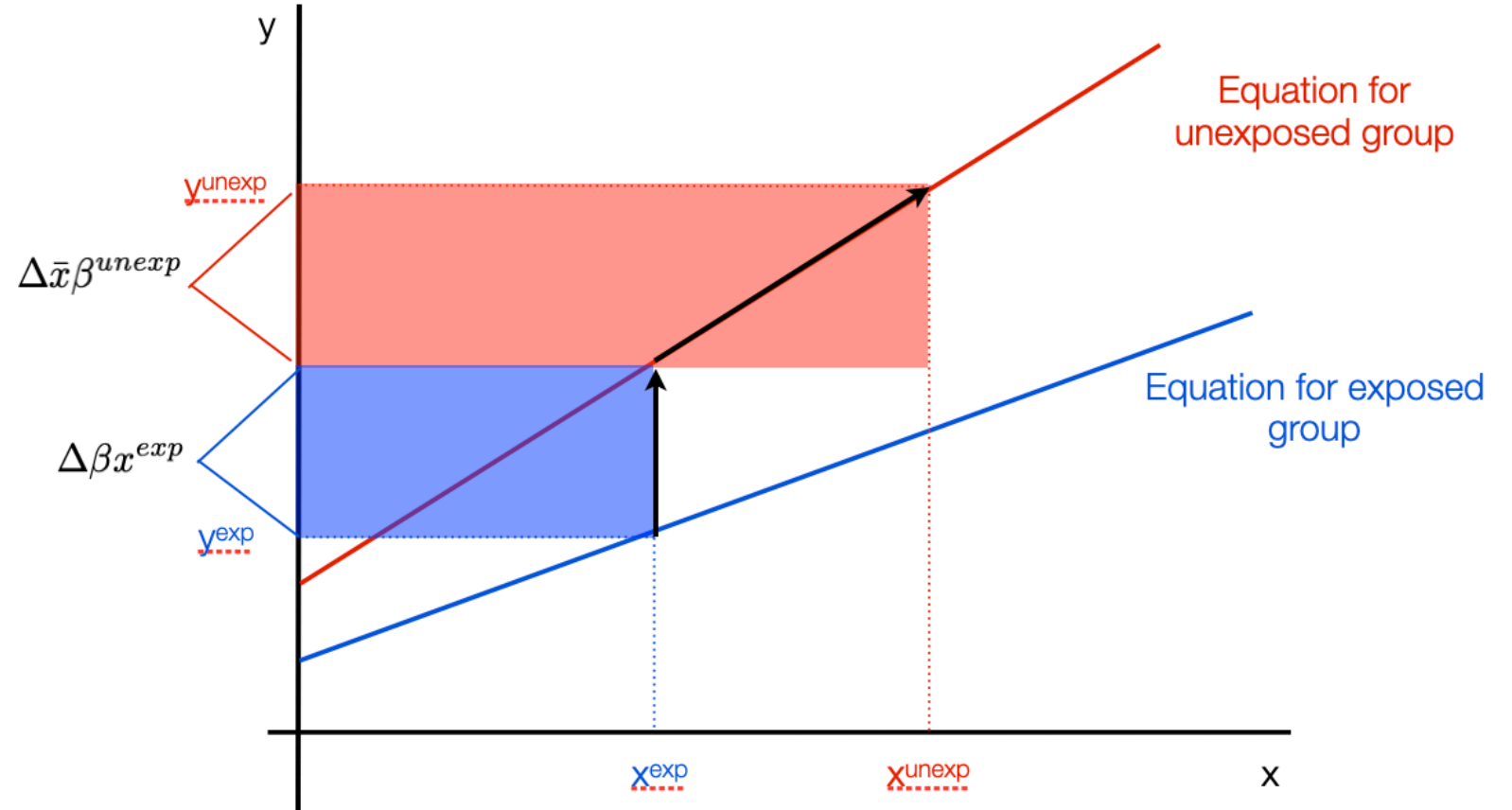
or, equivalently:

$$y^{exp} - y^{unexp} = \Delta \bar{x} \beta^{exp} + \Delta \beta x^{unexp}$$

First method

$$y^{exp} - y^{unexp} = \Delta \bar{x} \beta^{unexp} - \Delta \beta x^{exp}$$

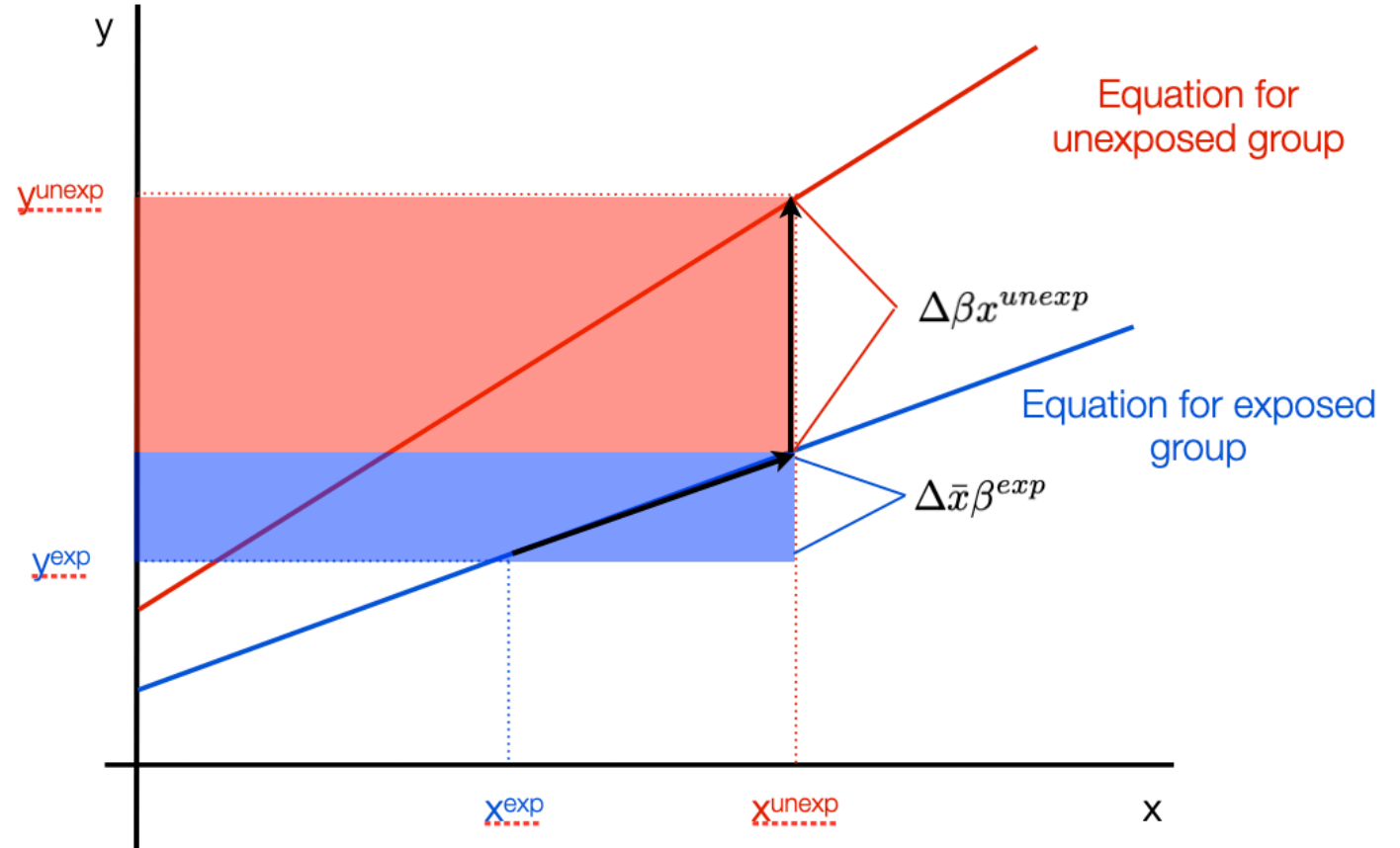
- Coefficients of unexposed
- Means of exposed



Second method

- Coefficients of exposed
- Means of unexposed

$$y^{exp} - y^{unexp} = \Delta \bar{x} \beta^{exp} - \Delta \beta x^{unexp}$$



The two methods are equally valid

In the first, the differences in the X s are weighted by the **coefficients of the unexposed group** and the differences in the coefficients are weighted by the X s of the exposed group:

$$y^{exp} - y^{unexp} = \Delta \bar{x} \beta^{unexp} - \Delta \beta x^{exp}$$

whereas, in the second, the differences in the X s are weighted by the **coefficients of the exposed group** and the differences in the coefficients are weighted by the X s of the unexposed group:

$$y^{exp} - y^{unexp} = \Delta \bar{x} \beta^{exp} - \Delta \beta x^{unexp}$$

Example: Decomposing Educational Differences in Blood Pressure

Basic question



What is the average difference in blood pressure between those with low vs. high education?

How much of this difference is due to the fact that determinants of blood pressure (e.g., BMI, smoking, demographics) differ between low and high educated groups?

Any residual difference is due to educational differences in the associations of risk factors for blood pressure.

Example data



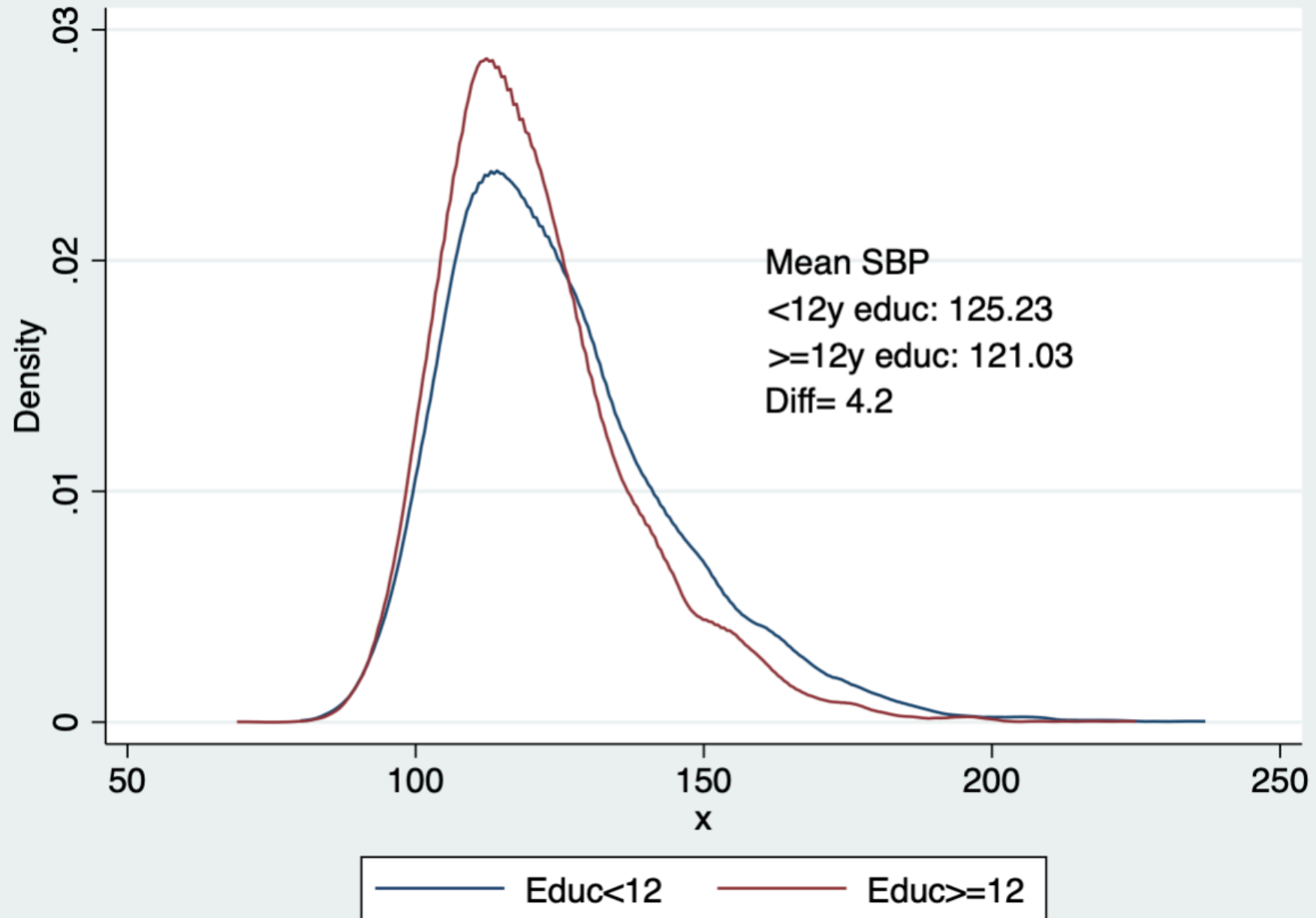
US NHANES follow up survey (1988-2006), baseline data

Systolic blood pressure as outcome (mmHg)

Overall difference by education (0: ≥ 12 y educ, 1: < 12 y educ)

Potential determinants (the Xs):

- age (years)
- age squared
- race (1 = non-white, 0 = other)
- marital status (1=married, 0=other)
- body mass index (kg/m^2)
- smoking (1=current smoker, 0=other)



Differences in determinants

- Lower educated have higher BMI and are more likely to be smokers, as well as being older

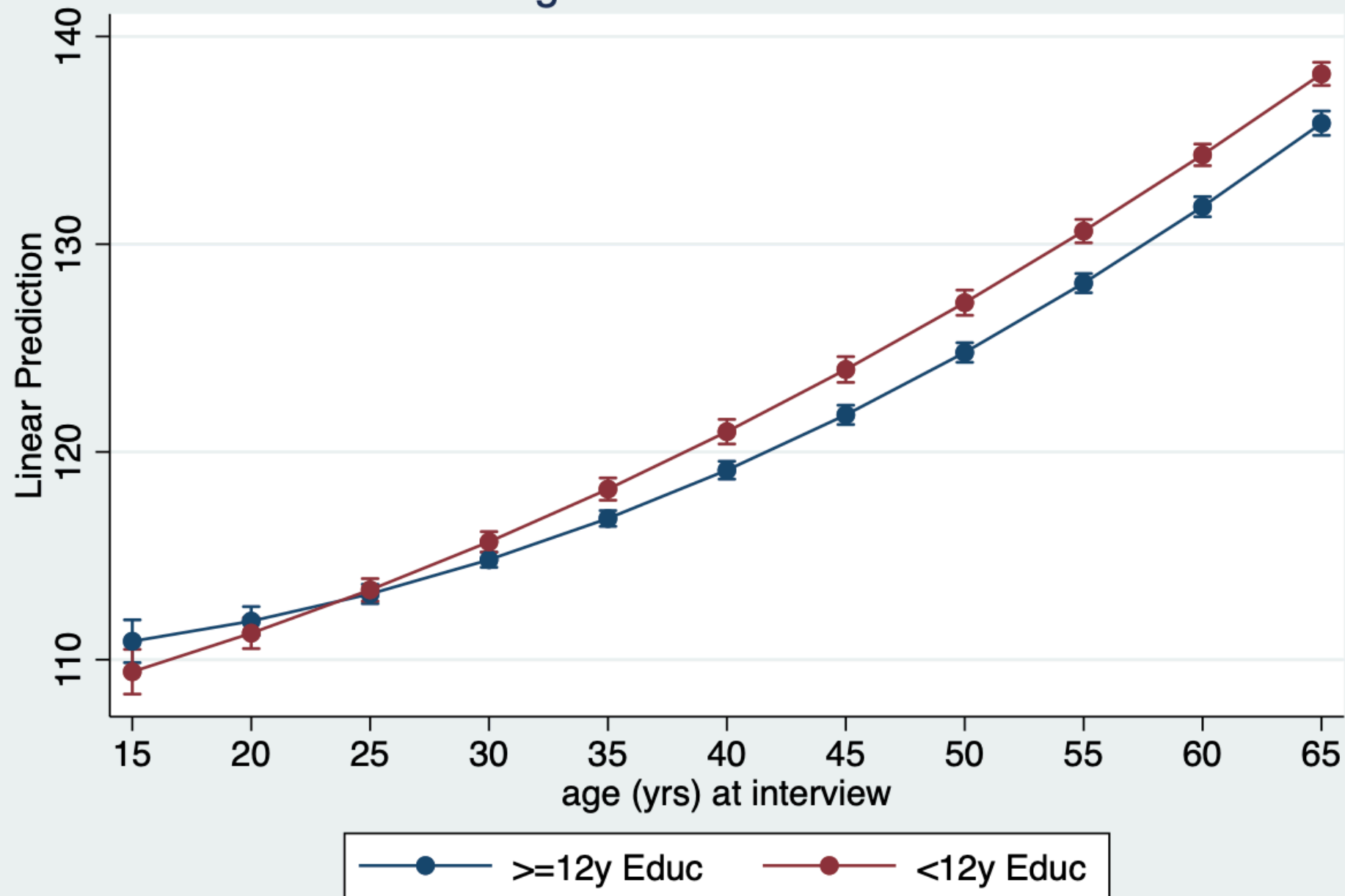
Variable	Covariate means			
	<12y Educ		>=12y Educ	
	\bar{x}	$SD(\bar{x})$	\bar{x}	$SD(\bar{x})$
Age	44.6	18.7	40.9	15.8
Age*Age	2338	1705	1920	1436
Non-white	0.33	0.47	0.36	0.48
Married	0.42	0.49	0.40	0.49
BMI	27.4	5.6	26.9	5.6
Smoker	0.31	0.46	0.25	0.43

Differences in coefficients

- BMI and smoking both have larger coefficients for the better educated group.
- Age has a slightly stronger association for the less educated.

Variable	Regression coefficients			
	<12y Educ		>=12y Educ	
	β	SE(β)	β	SE(β)
Age	0.60	0.01	0.53	0.01
Age*Age	0.00	0.00	0.01	0.00
Non-white	2.17	0.44	2.43	0.31
Married	0.92	0.44	0.89	0.32
BMI	0.38	0.04	0.61	0.02
Smoker	0.73	0.44	1.10	0.33
Intercept	110.86	1.11	102.20	0.74

Predictive Margins of educ12 with 95% CIs



		Coefficients used in decomposition:					
		<12y Educ		≥12y Educ		Pooled	
SBP (mmHg)		Est.	SE	Est.	SE	Est.	SE
≥12y Educ		121.03	0.17	121.03	0.17	121.03	0.17
<12y Educ		125.23	0.25	125.23	0.25	125.23	0.25
Difference		-4.20	0.30	-4.20	0.30	-4.20	0.30
Δ due to:							
Contribution of covariate differences	→ Covariate Means	-2.77	0.20	-2.88	0.19	-2.85	0.19
	Age	-2.14	0.17	-1.89	0.16	-2.00	0.16
	Age*Age	-0.46	0.08	-0.69	0.07	-0.59	0.06
	Non-white	0.07	0.02	0.07	0.02	0.07	0.02
	Married	-0.02	0.01	-0.02	0.01	-0.02	0.01
	BMI	-0.18	0.04	-0.29	0.06	-0.25	0.05
	Smoker	-0.04	0.03	-0.06	0.02	-0.06	0.02
Contribution of coefficient differences	→ Coefficients	-1.29	0.25	-1.40	0.26	-1.32	0.25
	Age	-0.13	0.03	0.11	0.03	-0.02	0.01
	Age*Age	0.79	0.35	0.56	0.25	0.69	0.32
	Non-white	0.08	0.18	0.09	0.19	0.08	0.19
	Married	-0.01	0.23	-0.01	0.21	-0.01	0.23
	BMI	0.06	0.02	-0.05	0.02	0.02	0.01
	Smoker	0.11	0.17	0.09	0.14	0.11	0.16
Interaction between coefficients and covariates	→ Interaction	-0.11	0.11	0.11	0.11		
	Intercept	-2.20	0.48	-2.20	0.48	-2.20	0.47

SBP (mmHg)	Coeffi	
	<12y Educ	
	Est.	SE
>=12y Educ	121.03	0.17
<12y Educ	125.23	0.25
Difference	-4.20	0.30
Δ due to:		
Covariate Means	-2.77	0.20
Age	-2.14	0.17
Age*Age	-0.46	0.08
Non-white	0.07	0.02
Married	-0.02	0.01
		0.04
		0.03
		0.25
		0.03
		0.35
		0.18
		0.23
		0.02
SMOKER	0.11	0.17
Intercept	-2.20	0.48
Interaction	-0.11	0.11

Contribution of covariate differences



SBP among the low educated group would be 2.8 mmHg lower if they had the same covariate characteristics as the higher educated.

Most of this difference comes from differences in the distribution of age.

Why positive? This means that the SBP difference would be even larger if the low educated had the same percentage non-white as the higher educated.

Variable	Covariate means			
	<12y Educ		>=12y Educ	
	\bar{x}	SD(\bar{x})	\bar{x}	SD(\bar{x})
Age	44.6	18.7	40.9	15.8
Age*Age	2338	1705	1920	1436
Non-white	0.33	0.47	0.36	0.48
Married	0.42	0.49	0.40	0.49
BMI	27.4	5.6	26.9	5.6
Smoker	0.31	0.46	0.25	0.43

Variable	Regression coefficients			
	<12y Educ		≥12y Educ	
	β	SE(β)	β	SE(β)
Age	0.60	0.01	0.53	0.01
Age*Age	0.00	0.00	0.01	0.00
Non-white	2.17	0.44	2.43	0.31
Married	0.92	0.44	0.89	0.32
BMI	0.38	0.04	0.61	0.02
Smoker	0.73	0.44	1.10	0.33
Intercept	110.86	1.11	102.20	0.74

	Coefficients	
	<12y Educ	≥12y Educ
	β	SE(β)
Age	0.60	0.01
Age*Age	0.00	0.00
Non-white	2.17	0.44
Married	0.92	0.44
BMI	0.38	0.04
Smoker	0.73	0.44
Intercept	110.86	1.11
Interaction	-0.11	0.11

Contribution of coefficient differences

→ Coefficients

SBP among the low educated group would be 1.3 mmHg lower if they had the same regression coefficients as the higher educated.

Most of this difference is captured by the intercept (i.e., unmeasured factors).

Why positive? This means that the SBP difference would be even larger if smoking had the same effect in low educated as it does in the higher educated.

SBP (mmHg)	Coefficients used in decomposition:					
	<12y Educ		≥12y Educ		Pooled	
	Est.	SE	Est.	SE	Est.	SE
≥12y Educ	121.03	0.17	121.03	0.17	121.03	0.17
<12y Educ	125.23	0.25	125.23	0.25	125.23	0.25
Difference	-4.20	0.30	-4.20	0.30	-4.20	0.30
Δ due to:						
Covariate Means	-2.77	0.20	-2.88	0.19	-2.85	0.19
Age	-2.14	0.17	-1.89	0.16	-2.00	0.16
Age*Age	-0.46	0.08	-0.69	0.07	-0.59	0.06
Non-white	0.07	0.02	0.07	0.02	0.07	0.02
Married	-0.02	0.01	-0.02	0.01	-0.02	0.01
BMI	-0.18	0.04	-0.29	0.06	-0.25	0.05
Smoker	-0.04	0.03	-0.06	0.02	-0.06	0.02
Coefficients	-1.29	0.25	-1.40	0.26	-1.32	0.25
Age	-0.13	0.03	0.11	0.03	-0.02	0.01
Age*Age	0.79	0.35	0.56	0.25	0.69	0.32
Non-white	0.08	0.18	0.09	0.19	0.08	0.19
Married	-0.01	0.23	-0.01	0.21	-0.01	0.23
BMI	0.06	0.02	-0.05	0.02	0.02	0.01
Smoker	0.11	0.17	0.09	0.14	0.11	0.16
Intercept	-2.20	0.48	-2.20	0.48	-2.20	0.47
Interaction	0.11	0.11	0.11	0.11		

Similar results if we use the coefficients of the higher educated to weight the covariate differences

SBP (mmHg)	Coefficients used in decomposition:					
	<12y Educ		≥12y Educ		Pooled	
	Est.	SE	Est.	SE	Est.	SE
≥12y Educ	121.03	0.17	121.03	0.17	121.03	0.17
<12y Educ	125.23	0.25	125.23	0.25	125.23	0.25
Difference	-4.20	0.30	-4.20	0.30	-4.20	0.30
Δ due to:						
Covariate Means	-2.77	0.20	-2.88	0.19	-2.85	0.19
Age	-2.14	0.17	-1.89	0.16	-2.00	0.16
Age*Age	-0.46	0.08	-0.69	0.07	-0.59	0.06
Non-white	0.07	0.02	0.07	0.02	0.07	0.02
Married	-0.02	0.01	-0.02	0.01	-0.02	0.01
BMI	-0.18	0.04	-0.29	0.06	-0.25	0.05
Smoker	-0.04	0.03	-0.06	0.02	-0.06	0.02
Coefficients	-1.29	0.25	-1.40	0.26	-1.32	0.25
Age	-0.13	0.03	0.11	0.03	-0.02	0.01
Age*Age	0.79	0.35	0.56	0.25	0.69	0.32
Non-white	0.08	0.18	0.09	0.19	0.08	0.19
Married	-0.01	0.23	-0.01	0.21	-0.01	0.23
BMI	0.06	0.02	-0.05	0.02	0.02	0.01
Smoker	0.11	0.17	0.09	0.14	0.11	0.16
Intercept	-2.20	0.48	-2.20	0.48	-2.20	0.47
Interaction	0.11	0.11	0.11	0.11		

Using coefficients from a model pooling both groups together also gives similar results.

No interaction term because only one set of coefficients is used for both group predictions.

Caveat: results depend on specification

Adding gender increases the “explained” component (i.e., “endowments”) from -2.77 to -2.95, so important consequences for how much of the gap is “unexplained”

```
. oaxaca systolic agec agec2 nonwhite married bmic current male, by(educ12) nodetail
```

```
Blinder-Oaxaca decomposition                Number of obs      =      15,859
                                           Model              =      linear
Group 1: educ12 = 0                        N of obs 1        =      9532
Group 2: educ12 = 1                        N of obs 2        =      6327
```

	<u>systolic</u>	<u>Coef.</u>	<u>Std. Err.</u>	<u>z</u>	<u>P> z </u>	<u>[95% Conf. Interval]</u>	
overall							
group_1		121.0268	.1744272	693.85	0.000	120.6849	121.3686
group_2		125.1985	.2500719	500.65	0.000	124.7084	125.6886
difference		-4.171762	.3048947	-13.68	0.000	-4.769345	-3.57418
endowments		-2.949963	.2080375	-14.18	0.000	-3.35771	-2.542217
coefficients		-1.023872	.2494773	-4.10	0.000	-1.512839	-.5349059
interaction		-.1979264	.1126793	-1.76	0.079	-.4187737	.0229209

Methods frontier

- Attempting to reconcile the non-causal framework of KBO with mediation methods, new estimators.

Meaningful Causal Decompositions in Health Equity Research

Definition, Identification, and Estimation Through a Weighting Framework

John W. Jackson^{a,b,c,d,e}

Abstract: Causal decomposition analyses can help build the evidence base for interventions that address health disparities (inequities). They ask how disparities in outcomes may change under hypothetical intervention. Through study design and assumptions, they can rule out alternate explanations such as confounding, selection bias, and measurement error, thereby identifying potential targets for intervention. Unfortunately, the literature on causal decomposition analysis and related methods have largely ignored equity concerns that actual interventionists would respect, limiting their relevance and practical value. This article addresses these concerns by explicitly considering what covariates the outcome disparity and hypothetical intervention adjust for (so-called allowable covariates) and the equity value judgments

(Epidemiology 2021;32: 282–290)

Health disparities represent differences across privileged versus socially marginalized groups that are considered inequitable, avoidable, and unjust.¹ Interventions that address disparities² usually affect risk factors overrepresented among marginalized groups. The evidence base draws from studies that compare disparities before and after adjustment for a risk difference method³). But the changes seen after

Summary



Various decomposition techniques exist that may be useful for analyzing social determinants of health Life table decomposition—over time or between groups, or both Regression-based decomposition of Concentration Index Oaxaca decomposition of mean health between groups

All of these techniques make assumptions that need to be evaluated in the course of analysis

When used properly, decomposition techniques can help to provide key evidence on why health inequalities exist and change over time.